

Spatial Index Structures

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Outline

- ✧ Introduction
- ✧ Spatial Indexing
- ✧ R-Tree
- ✧ R⁺-Tree
- ✧ Quad Trees

Introduction

- ✚ Spatial objects
 - Points, lines, rectangles, regions, ...
- ✚ Hierarchical data structures
 - Based on recursive decomposition, similar to divide and conquer method, like B-tree.
- ✚ Why not B-Tree?
 - More than one dimension
 - Concept of closeness relies on all the dimensions of the spatial data
- ✚ Spatial index structures demo
 - <http://www.cs.umd.edu/~brabec/quadtree/index.html>

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Spatial Indexing

- ✚ Mapping spatial object into point
 - In either same, lower, or higher dimensional spaces
 - Good for storage purposes
 - Problems with queries like finding the nearest objects
 - ✚ Bucketing methods
 - Based on spatial occupancy
 - Decomposing the space from which the data is drawn
 - Minimum bounding rectangle (MBR) : e.g., R-Tree
 - Disjoint cells: e.g., R⁺-Tree
 - Blocks of uniform size
 - Distribution of the data: e.g., quadtree
- } data-dependent
} greater degree of data-independence

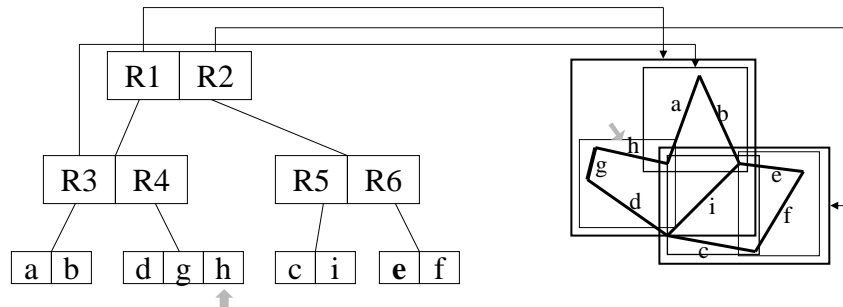
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R-Tree

[proposed in 1984 by Guttman]

✂ Based on Minimum Bounding Rectangle

$(m, M) = (1, 3)$



- bounding rectangles could overlap each others (e.g., R3 vs R4)
- an object is only associated with one bounding rectangle

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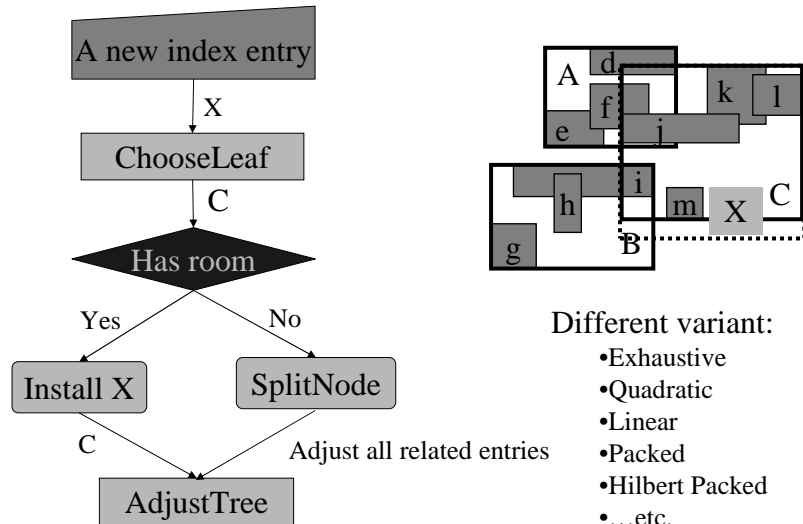
R-Tree

[proposed in 1984 by Guttman]

- ✂ Height-balanced tree similar to B-tree for k -dimensions
- ✂ Every leaf node contains between m ($m \leq M/2$) and M index records, unless it is the root
- ✂ For each index record $(I, \text{tuple-identifier})$ in a leaf node, I is the MBR that contains the n -dimensional data object represented by the indicated tuple
- ✂ Every non-leaf node has between m and M children unless it is the root
- ✂ For each entry $(I, \text{child-pointer})$ in a non-leaf node, I is the MBR that spatially contains the rectangles in the child node.
- ✂ All leaves appear on the same level
- ✂ The root node has at least two children unless it is a leaf

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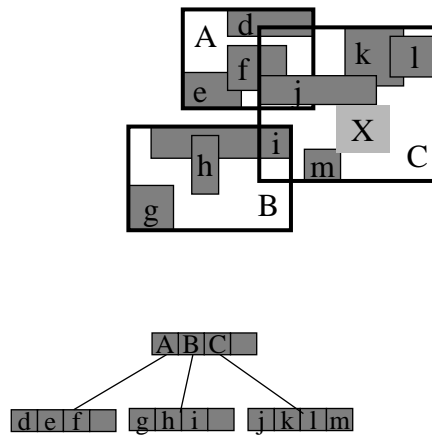
Insertion Processes



Processes of Quadratic Spilt

(page 52 in Guttman's paper)

Pick first entry for each group
Run PickSeeds



Processes of Quadratic Spilt

(page 52 in Guttman's paper)

PickSeeds

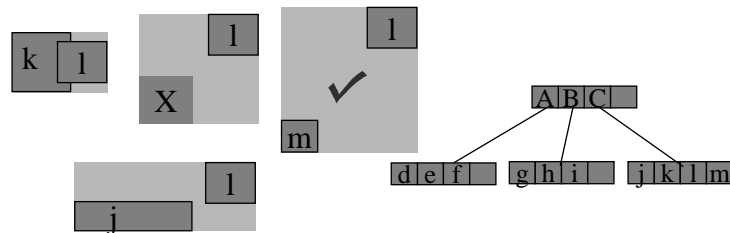
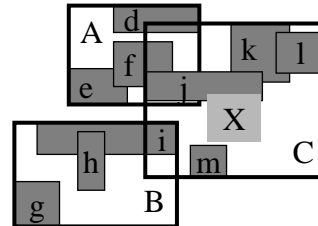
PS1 [Calculate inefficiency of grouping entries together]

For each pair of E1 and E2, compose a rectangle R including E1 and E2

Calculate $d = \text{area}(R) - \text{area}(E1) - \text{area}(E2)$

PS2 [Choose the most wasteful pair]

Choose the pair with the largest d



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Processes of Quadratic Spilt

(page 52 in Guttman's paper)

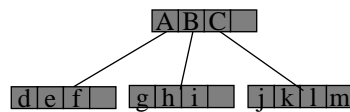
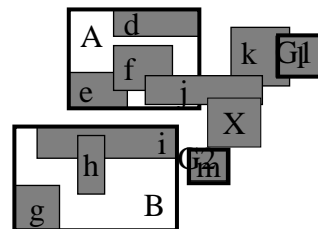
Pick first entry for each group
(PickSeeds)

G1	G2
l	m

Check if done

No

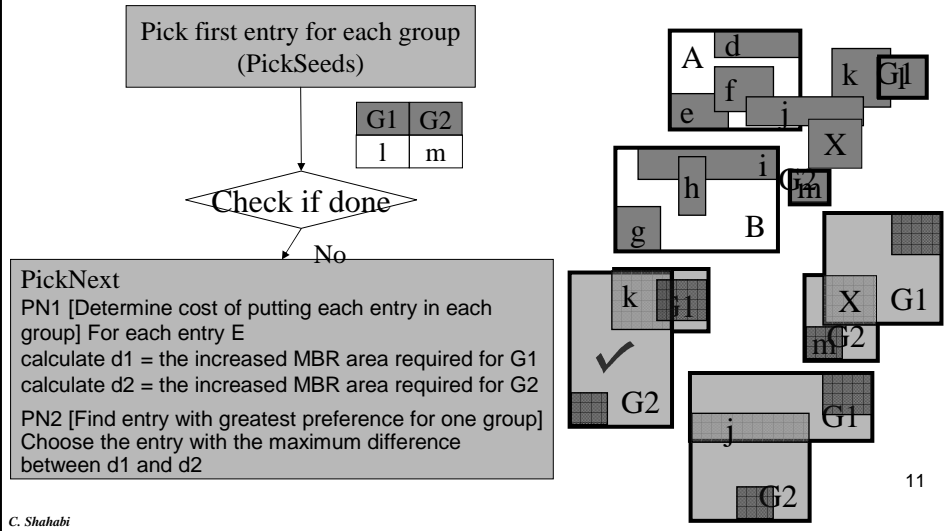
Select entry to assign
(PickNext)



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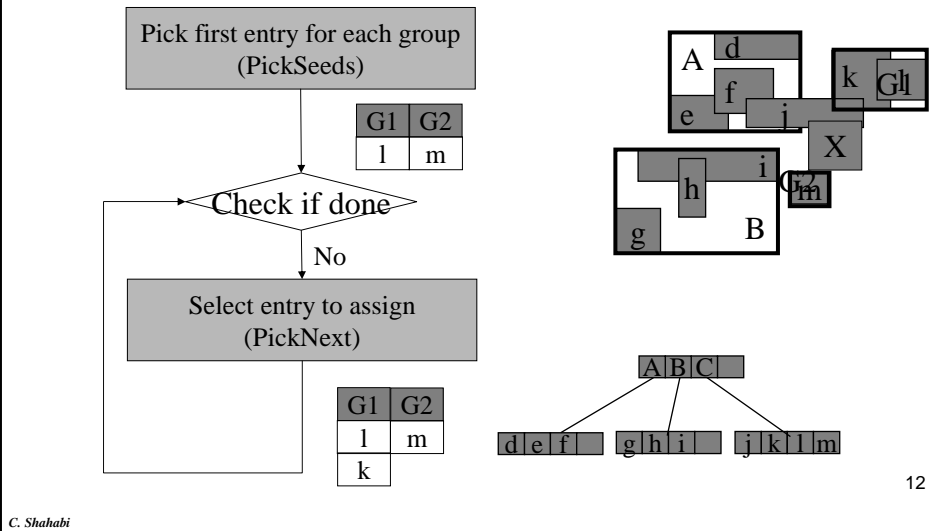
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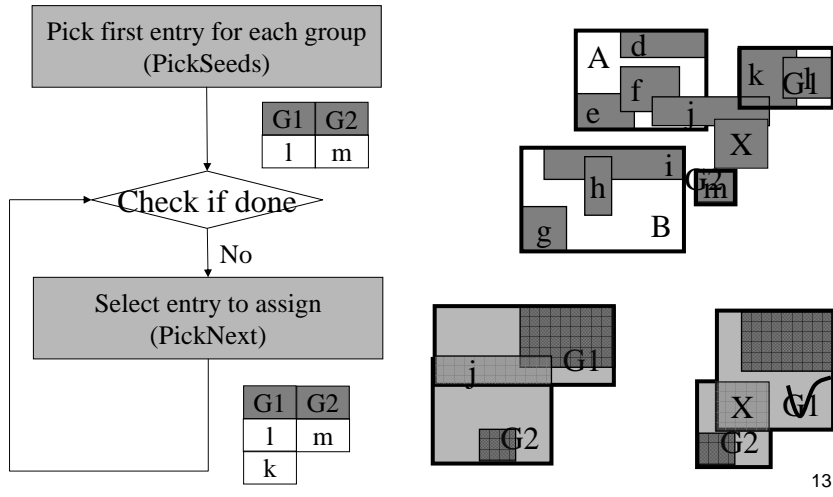
Processes of Quadratic Spilt

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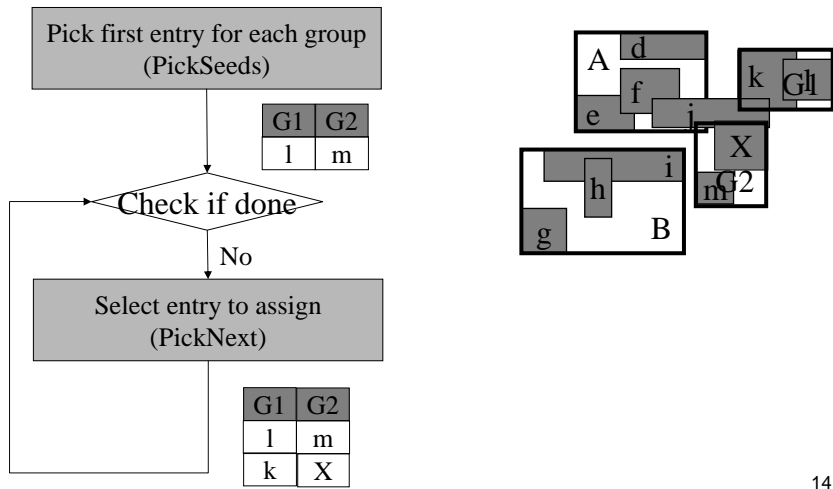
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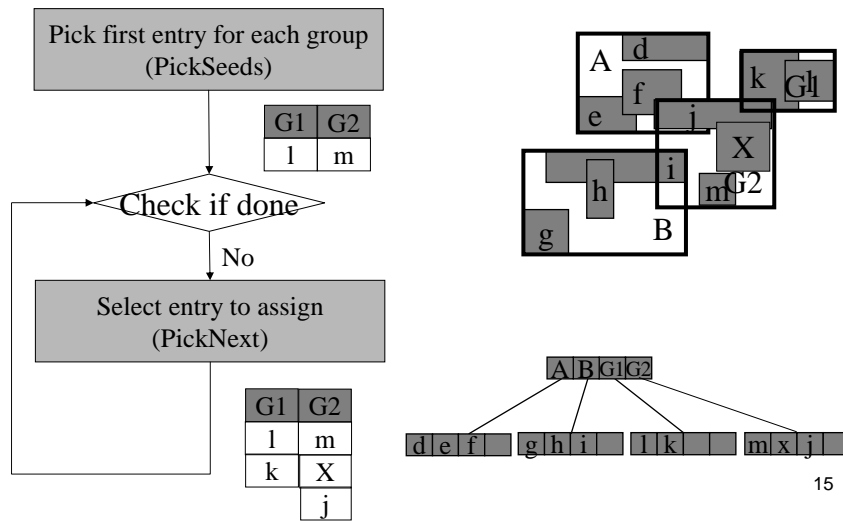
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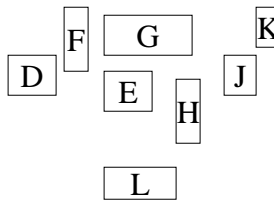
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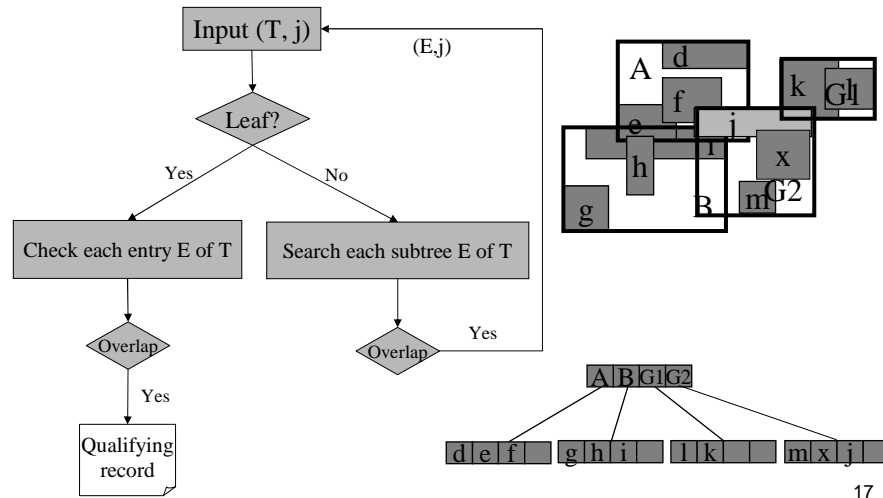
Your Exercise Before Midterm

✎ $(m, M) = (2, 4)$



- ✎ Build a R-Tree for these spatial data
- ✎ Hint: You could use the Spatial index structures demo application step by step

Search Object in R-Tree

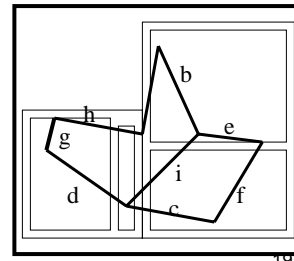
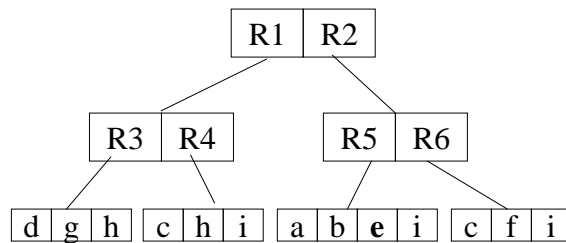


Main Drawbacks of R-Tree

- ✘ R-tree is not unique, rectangles depend on how objects are inserted and deleted from the tree.
- ✘ In order to search some object you might have to go through several rectangles or the whole database
 - Why?
 - Solution?

R⁺-Tree

- ✎ Overcome problems with R-Tree
- ✎ If node overlaps with several rectangles insert the node in all
- ✎ Decompose the space into disjoint cells



R⁺-Tree Properties

- ✎ R⁺-tree and cell-trees used approach of decomposing space into cells
 - R⁺-trees deals with collection of objects bounded by rectangles
 - Cell tree deals with collection of objects bounded by convex polyhedron
- ✎ R⁺-trees is extension of k-d-B-tree
- ✎ Retrieval times are smaller
- ✎ When summing the objects, needs eliminate duplicates
- ✎ Again, it is data-dependent

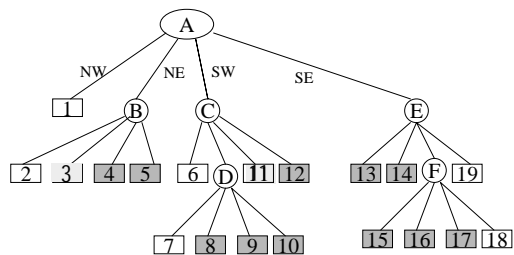
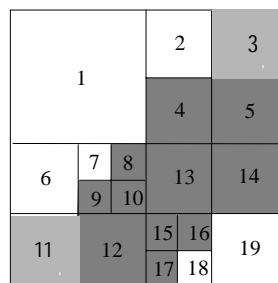
Quad Trees

Region Quadtree

- The blocks are required to be disjoint
- Have standard sizes (squares whose sides are power of two)
- At standard locations
- Based on successive subdivision of image array into four equal-size quadrants
- If the region does not cover the entire array, subdivide into quadrants, sub-quadrants, etc.
- A variable resolution data structure

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Example of Region Quadtree

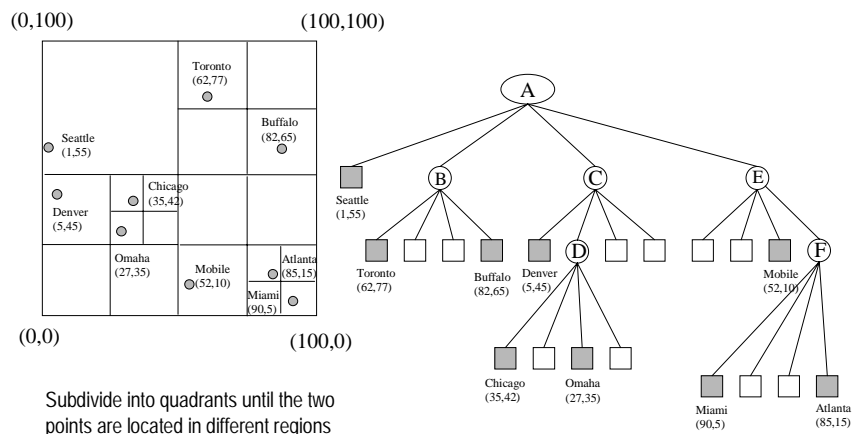


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PR Quadtree

- ✂ PR (Point-Region) quadtree
- ✂ Regular decomposition (similar to Region quadtree)
- ✂ Independent of the order in which data points are inserted into it
- ✂ ☹: if two points are very close, decomposition can be very deep

Example of PR Quadtree



PM Quadtree

PM (Polygonal-Map) quadtree family

- PM1 quadtree, PM2 quadtree, PM3 quadtree, PMR quadtree, ... etc.

PM1 quadtree

- Based on regular decomposition of space
- Vertex-based implementation
- Criteria
 - At most one vertex can lie in a region represented by a quadtree leaf
 - If a region contains a vertex, it can contain no partial-edge that does not include that vertex
 - If a region contains no vertices, it can contain at most one partial-edge



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PM Quadtree

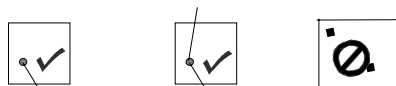
PM1 quadtree



PM2 quadtree

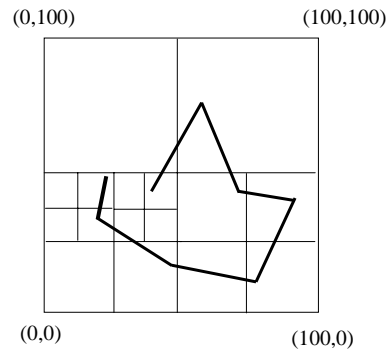


PM3 quadtree



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Example of PM1 Quadtree



- ✦ Each node in a PM quadtree is a collection of partial edges (and a vertex)
- ✦ Each point record has two field (x,y)
- ✦ Each partial edge has four field (starting_point, ending_point, left region, right region)

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Question?

✦ Question?

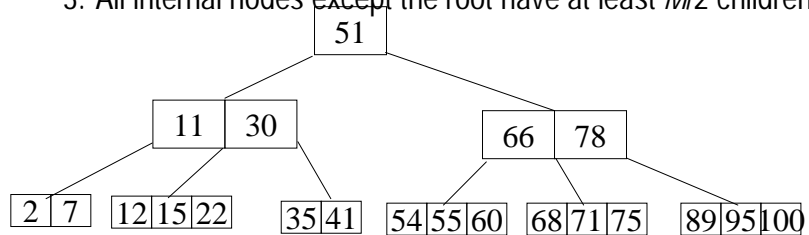
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B-Tree: Definition

A B-Tree of order M is a height-balanced tree

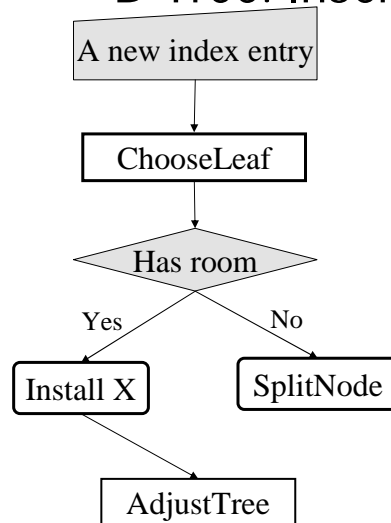
1. All leaves are on the same level
2. All nodes have at most M children
3. All internal nodes except the root have at least $M/2$ children

=m



Back to R+ Tree
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B-Tree: Insertion



back