

Distributed Databases

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Excerpt from “Principles of Distributed Database Systems”
by M. Tamer Özsu and Patrick Valduriez

Topics

- Introduction
- Background
- Distributed DBMS Architecture
- Distributed Database Design
- Semantic Data Control
- Distributed Query Processing
- Distributed Transaction Management
- Parallel Database Systems
- Distributed Object DBMS
- Database Interoperability
- Current Issues

Outline

- ❑ Design what?
- ❑ Fragmentation
- ❑ Allocation

Design Approaches

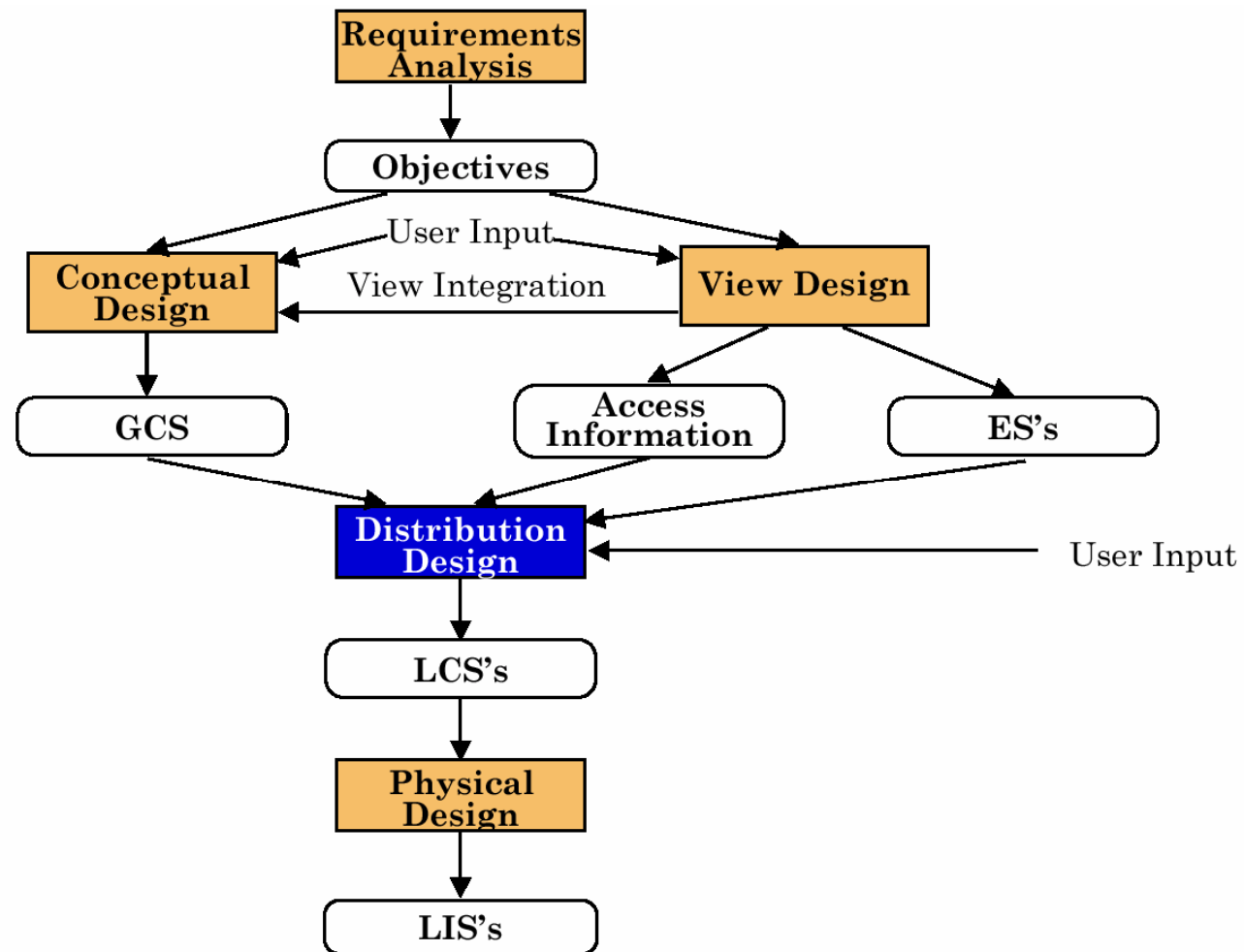
■ Top-down

- ➡ mostly in designing systems from scratch
- ➡ mostly in homogeneous systems

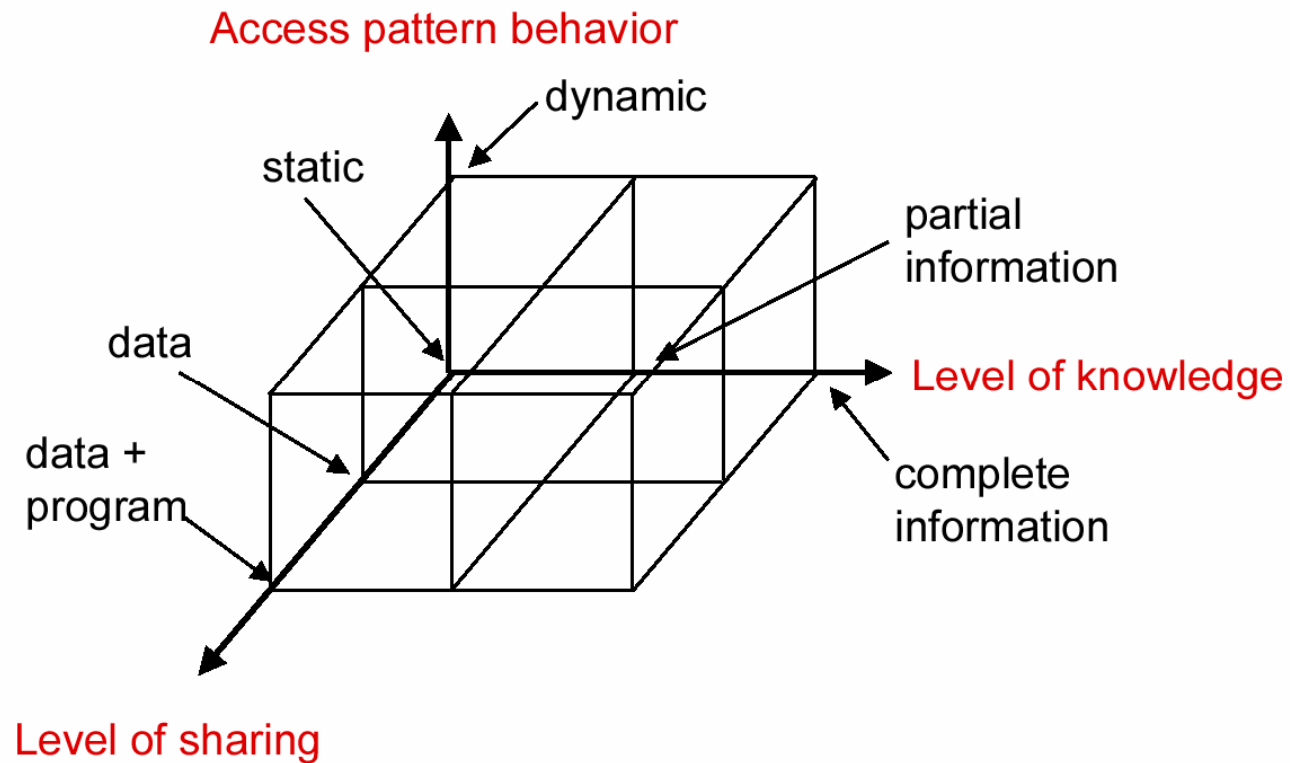
■ Bottom-up

- ➡ when the databases already exist at a number of sites

Top-Down Design



Dimensions of the Design Problem



Distribution Design Issues

- ❶ Why fragment at all?
- ❷ How to fragment?
- ❸ How much to fragment?
- ❹ How to test correctness?
- ❺ How to allocate?
- ❻ Information requirements?

Fragmentation

- Can't we just distribute relations?
- What is a reasonable unit of distribution?
 - ▢ relation
 - ◆ views are subsets of relations; partition to achieve locality
 - ◆ extra communication
 - ▢ fragments of relations (sub-relations)
 - ◆ concurrent execution of a number of transactions that access different portions of a relation
 - ◆ views that cannot be defined on a single fragment will require extra processing
 - ◆ semantic data control (especially integrity enforcement) more difficult

Fragmentation Alternatives - Horizontal

PROJ₁ : projects with budgets less than \$200,000

PROJ₂ : projects with budgets greater than or equal to \$200,000

PROJ

PNO	PNAME	BUDGET	LOC
P1	Instrumentation	150000	Montreal
P2	Database Develop.	135000	New York
P3	CAD/CAM	250000	New York
P4	Maintenance	310000	Paris
P5	CAD/CAM	500000	Boston

PROJ₁

PNO	PNAME	BUDGET	LOC
P1	Instrumentation	150000	Montreal
P2	Database Develop.	135000	New York

PROJ₂

PNO	PNAME	BUDGET	LOC
P3	CAD/CAM	250000	New York
P4	Maintenance	310000	Paris
P5	CAD/CAM	500000	Boston

Fragmentation Alternatives - Vertical

PROJ₁: information about
project budgets

PROJ₂: information about
project names and
locations

PROJ

PNO	PNAME	BUDGET	LOC
P1	Instrumentation	150000	Montreal
P2	Database Develop.	135000	New York
P3	CAD/CAM	250000	New York
P4	Maintenance	310000	Paris
P5	CAD/CAM	500000	Boston

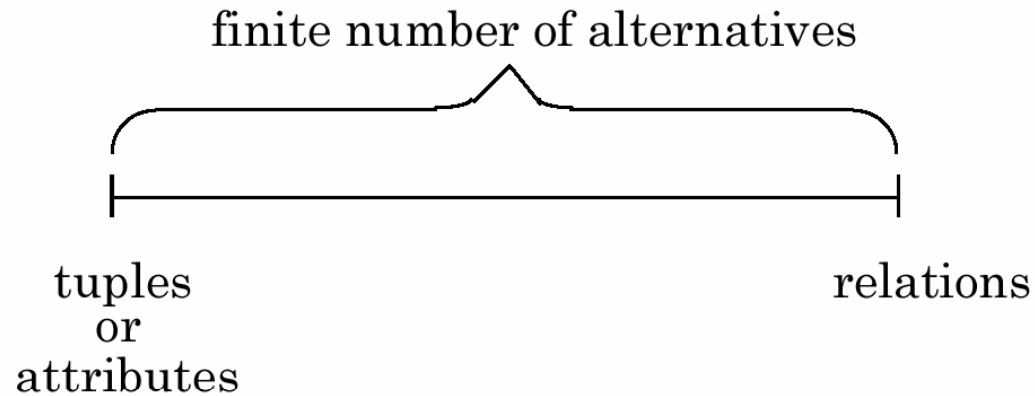
PROJ₁

PNO	BUDGET
P1	150000
P2	135000
P3	250000
P4	310000
P5	500000

PROJ₂

PNO	PNAME	LOC
P1	Instrumentation	Montreal
P2	Database Develop.	New York
P3	CAD/CAM	New York
P4	Maintenance	Paris
P5	CAD/CAM	Boston

Degree of Fragmentation



Finding the suitable level of partitioning within this range

Correctness of Fragmentation

■ Completeness

- ➡ Decomposition of relation R into fragments R_1, R_2, \dots, R_n is complete if and only if each data item in R can also be found in some R_i

■ Reconstruction

- ➡ If relation R is decomposed into fragments R_1, R_2, \dots, R_n , then there should exist some relational operator ∇ such that

$$R = \nabla_{1 \leq i \leq n} R_i$$

■ Disjointness

- ➡ If relation R is decomposed into fragments R_1, R_2, \dots, R_n , and data item d_i is in R_j , then d_i should not be in any other fragment R_k ($k \neq j$).

Allocation Alternatives

- Non-replicated

- ▶ partitioned : each fragment resides at only one site

- Replicated

- ▶ fully replicated : each fragment at each site
 - ▶ partially replicated : each fragment at some of the sites

- Rule of thumb:

If $\frac{\text{read - only queries}}{\text{update queries}} \geq 1$ replication is advantageous,

otherwise replication may cause problems

Information Requirements

- Four categories:

- Database information
- Application information
- Communication network information
- Computer system information

Outline

- Design what?
- Fragmentation
- Allocation

Fragmentation

- Horizontal Fragmentation (HF)
 - ▶ Primary Horizontal Fragmentation (PHF)
 - ▶ Derived Horizontal Fragmentation (DHF)
- Vertical Fragmentation (VF)
- Hybrid Fragmentation (HF)

Our Running Example

EMP

ENO	ENAME	TITLE
E1	J. Doe	Elect. Eng.
E2	M. Smith	Syst. Anal.
E3	A. Lee	Mech. Eng.
E4	J. Miller	Programmer
E5	B. Casey	Syst. Anal.
E6	L. Chu	Elect. Eng.
E7	R. Davis	Mech. Eng.
E8	J. Jones	Syst. Anal.

ASG

ENO	PNO	RESP	DUR
E1	P1	Manager	12
E2	P1	Analyst	24
E2	P2	Analyst	6
E3	P3	Consultant	10
E3	P4	Engineer	48
E4	P2	Programmer	18
E5	P2	Manager	24
E6	P4	Manager	48
E7	P3	Engineer	36
E7	P5	Engineer	23
E8	P3	Manager	40

PROJ

PNO	PNAME	BUDGET
P1	Instrumentation	150000
P2	Database Develop	135000
P3	CAD/CAM	250000
P4	Maintenance	310000

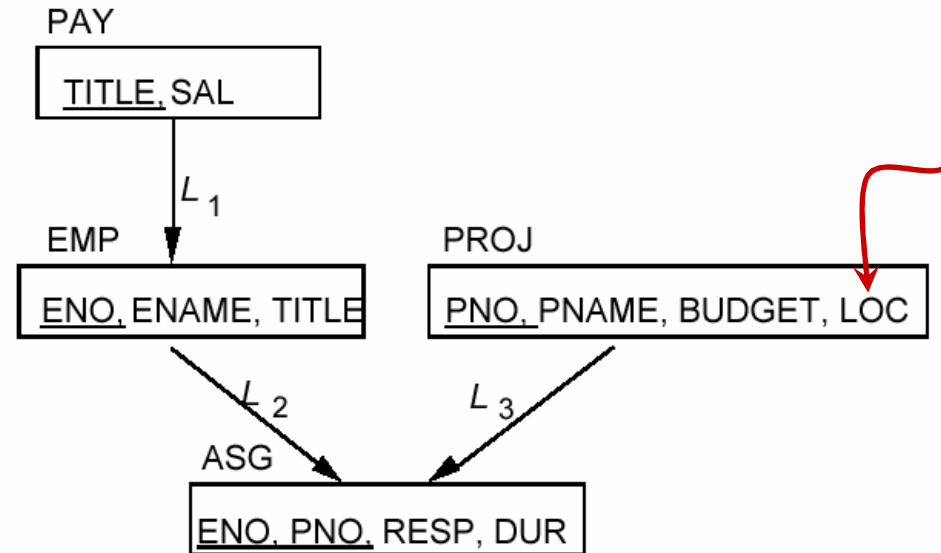
PAY

TITLE	SAL
Elect. Eng.	40000
Syst. Anal.	34000
Mech. Eng.	27000
Programmer	24000

PHF – Information Requirements

■ Database Information

➡ relationship



➡ cardinality of each relation: $card(R)$

PHF – Information Requirements

■ Application Information

➡ **simple predicates** : Given $R[A_1, A_2, \dots, A_n]$, a simple predicate p_j is

$$p_j : A_i \theta \text{ Value}$$

where $\theta \in \{=, <, \leq, >, \geq, \neq\}$, $\text{Value} \in D_i$ and D_i is the domain of A_i .

For relation R we define $Pr = \{p_1, p_2, \dots, p_m\}$

Example :

PNAME = "Maintenance"

BUDGET \leq 200000

➡ **minterm predicates** : Given R and $Pr = \{p_1, p_2, \dots, p_m\}$

define $M = \{m_1, m_2, \dots, m_r\}$ as

$$M = \{ m_i \mid m_i = \bigwedge_{p_j \in Pr} p_j^* \}, 1 \leq j \leq m, 1 \leq i \leq r$$

where $p_j^* = p_j$ or $p_j^* = \neg(p_j)$.

PHF – Information Requirements

Example

m_1 : PNAME="Maintenance" \wedge BUDGET \leq 200000

m_2 : **NOT**(PNAME="Maintenance") \wedge BUDGET \leq 200000

m_3 : PNAME= "Maintenance" \wedge **NOT**(BUDGET \leq 200000)

m_4 : **NOT**(PNAME="Maintenance") \wedge **NOT**(BUDGET \leq 200000)

PHF – Information Requirements

■ Application Information

▢ **minterm selectivities:** $sel(m_i)$

- ◆ The number of tuples of the relation that would be accessed by a user query which is specified according to a given minterm predicate m_i .

▢ **access frequencies:** $acc(q_i)$

- ◆ The frequency with which a user application q_i accesses data.
- ◆ Access frequency for a minterm predicate can also be defined.

Primary Horizontal Fragmentation

Definition :

$$R_j = \sigma_{F_j}(R), \quad 1 \leq j \leq w$$

where F_j is a selection formula, which is (preferably) a minterm predicate.

Therefore,

A horizontal fragment R_i of relation R consists of all the tuples of R which satisfy a minterm predicate m_i .

Given a set of minterm predicates M , there are as many horizontal fragments of relation R as there are minterm predicates.

Set of horizontal fragments also referred to as *minterm fragments*.

Selecting Simple Predicates

Given: A relation R , the set of simple predicates Pr

Output: The set of fragments of $R = \{R_1, R_2, \dots, R_w\}$
which obey the fragmentation rules.

Preliminaries :

⇒ Pr should be *complete*

⇒ Pr should be *minimal*

Completeness of Simple Predicates

- A set of simple predicates Pr is said to be *complete* if and only if the accesses to the tuples of the minterm fragments defined on Pr requires that two tuples of the same minterm fragment have the same probability of being accessed by any application.

- Example :
 - ▶▶▶ Assume PROJ[PNO,PNAME,BUDGET,LOC] has two applications defined on it.
 - ▶▶▶ Find the budgets of projects at each location. (1)
 - ▶▶▶ Find projects with budgets less than \$200000. (2)

Completeness of Simple Predicates

According to (1),

$$Pr = \{LOC = \text{"Montreal"}, LOC = \text{"New York"}, LOC = \text{"Paris"}\}$$

which is not complete with respect to (2).

Modify

$$Pr = \{LOC = \text{"Montreal"}, LOC = \text{"New York"}, LOC = \text{"Paris"}, \\ BUDGET \leq 200000, BUDGET > 200000\}$$

which is complete.

Minimality of Simple Predicates

- If a predicate influences how fragmentation is performed, (i.e., causes a fragment f to be further fragmented into, say, f_i and f_j) then there should be at least one application that accesses f_i and f_j differently.
- In other words, the simple predicate should be *relevant* in determining a fragmentation.
- If all the predicates of a set Pr are relevant, then Pr is *minimal*.

Minimality of Simple Predicates

Example :

$$Pr = \{ \text{LOC} = \text{"Montreal"}, \text{LOC} = \text{"New York"}, \text{LOC} = \text{"Paris"}, \\ \text{BUDGET} \leq 200000, \text{BUDGET} > 200000 \}$$

is minimal (in addition to being complete).
However, if we add

$$\text{PNAME} = \text{"Instrumentation"}$$

then Pr is not minimal.

COM_MIN Algorithm

Given: a relation R and a set of simple predicates Pr

Output: a *complete* and *minimal* set of simple predicates Pr' for Pr

Rule 1: a relation or fragment is partitioned into at least two parts which are accessed differently by at least one application.

COM_MIN Algorithm

① Initialization :

- find a $p_i \in Pr$ such that p_i partitions R according to *Rule 1*
- set $Pr' = p_i$; $Pr \leftarrow Pr - p_i$; $F \leftarrow f_i$

② Iteratively add predicates to Pr' until it is complete

- find a $p_j \in Pr$ such that p_j partitions some f_k defined according to minterm predicate over Pr' according to *Rule 1*
- set $Pr' = Pr' \cup p_j$; $Pr \leftarrow Pr - p_j$; $F \leftarrow F \cup f_j$
- if $\exists p_k \in Pr'$ which is nonrelevant then
$$Pr' \leftarrow Pr' - p_k$$
$$F \leftarrow F - f_k$$

PHORIZANTAL Algorithm

Makes use of COM_MIN to perform fragmentation.

Input: a relation R and a set of simple predicates Pr

Output: a set of minterm predicates M according to which relation R is to be fragmented

- ① $Pr' \leftarrow \text{COM_MIN}(R, Pr)$
- ② determine the set M of minterm predicates
- ③ determine the set I of implications among $p_i \in Pr$
- ④ eliminate the contradictory minterms from M

Examples

- Two candidate relations : PAY and PROJ.

- Fragmentation of relation PAY

- ➡ Application: Check the salary info and determine raise.

- ➡ Employee records kept at two sites application run at two sites

- ➡ Simple predicates

- $p_1 : \text{SAL} \leq 30000$

- $p_2 : \text{SAL} > 30000$

- $Pr = \{p_1, p_2\}$ which is complete and minimal $Pr' = Pr$

- ➡ Minterm predicates

- $m_1 : (\text{SAL} \leq 30000)$

- $m_2 : \text{NOT}(\text{SAL} \leq 30000) = (\text{SAL} > 30000)$

PAY

TITLE	SAL
Elect. Eng.	40000
Syst. Anal.	34000
Mech. Eng.	27000
Programmer	24000

Examples

PAY₁

TITLE	SAL
Mech. Eng.	27000
Programmer	24000

PAY₂

TITLE	SAL
Elect. Eng.	40000
Syst. Anal.	34000

Examples

■ Fragmentation of relation PROJ

➤ Applications:

- ◆ Find the name and budget of projects given their no.
 - ✓ Issued at three sites
- ◆ Access project information according to budget
 - ✓ one site accesses ≤ 200000 other accesses > 200000

➤ Simple predicates

➤ For application (1)

$p_1 : \text{LOC} = \text{"Montreal"}$
 $p_2 : \text{LOC} = \text{"New York"}$
 $p_3 : \text{LOC} = \text{"Paris"}$

➤ For application (2)

$p_4 : \text{BUDGET} \leq 200000$
 $p_5 : \text{BUDGET} > 200000$

➤ $Pr = Pr' = \{p_1, p_2, p_3, p_4, p_5\}$

PROJ

PNO	PNAME	BUDGET	LOC
P1	Instrumentation	150000	Montreal
P2	Database Develop	135000	New York
P3	CAD/CAM	250000	New York
P4	Maintenance	310000	Paris

Examples

■ Fragmentation of relation PROJ continued

➡ Minterm fragments left after elimination

$$m_1 : (\text{LOC} = \text{"Montreal"}) \wedge (\text{BUDGET} \leq 200000)$$

$$m_2 : (\text{LOC} = \text{"Montreal"}) \wedge (\text{BUDGET} > 200000)$$

$$m_3 : (\text{LOC} = \text{"New York"}) \wedge (\text{BUDGET} \leq 200000)$$

$$m_4 : (\text{LOC} = \text{"New York"}) \wedge (\text{BUDGET} > 200000)$$

$$m_5 : (\text{LOC} = \text{"Paris"}) \wedge (\text{BUDGET} \leq 200000)$$

$$m_6 : (\text{LOC} = \text{"Paris"}) \wedge (\text{BUDGET} > 200000)$$

$i_1:$	$p_1 \Rightarrow \neg p_2 \wedge \neg p_3$
$i_2:$	$p_2 \Rightarrow \neg p_1 \wedge \neg p_3$
$i_3:$	$p_3 \Rightarrow \neg p_1 \wedge \neg p_2$
$i_4:$	$p_4 \Rightarrow \neg p_5$
$i_5:$	$p_5 \Rightarrow \neg p_4$
$i_6:$	$\neg p_4 \Rightarrow p_5$
$i_7:$	$\neg p_5 \Rightarrow p_4$

Examples

PROJ₁

PNO	PNAME	BUDGET	LOC
P1	Instrumentation	150000	Montreal

PROJ₂

PNO	PNAME	BUDGET	LOC
P2	Database Develop.	135000	New York

PROJ₄

PNO	PNAME	BUDGET	LOC
P3	CAD/CAM	250000	New York

PROJ₆

PNO	PNAME	BUDGET	LOC
P4	Maintenance	310000	Paris

Correctness

■ Completeness

- ⇒ Since Pr' is complete and minimal, the selection predicates are complete

■ Reconstruction

- ⇒ If relation R is fragmented into $F_R = \{R_1, R_2, \dots, R_r\}$

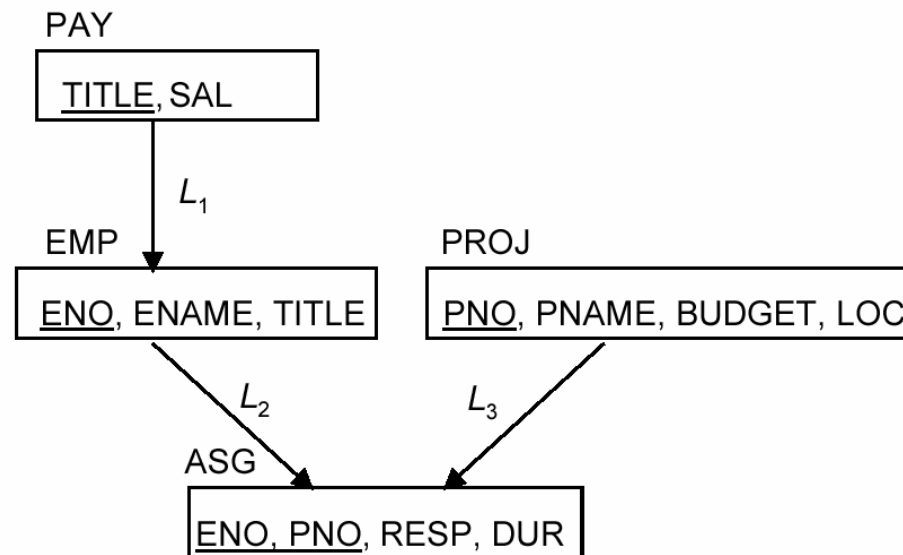
$$R = \cup_{R_i \in F_R} R_i$$

■ Disjointness

- ⇒ Minterm predicates that form the basis of fragmentation should be mutually exclusive.

Derived Horizontal Fragmentation

- Defined on a member relation of a link according to a selection operation specified on its owner.
 - ➡ Each link is an equijoin.
 - ➡ Equijoin can be implemented by means of semijoins.



Definition

Given a link L where $owner(L)=S$ and $member(L)=R$, the derived horizontal fragments of R are defined as

$$R_i = R \bowtie S_i, \quad 1 \leq i \leq w$$

where w is the maximum number of fragments that will be defined on R and

$$S_i = \sigma_{F_i}(S)$$

where F_i is the formula according to which the primary horizontal fragment S_i is defined.

Example

Given link L_1 where $\text{owner}(L_1)=\text{PAY}$ and $\text{member}(L_1)=\text{EMP}$

$$\text{EMP}_1 = \text{EMP} \bowtie \text{PAY}_1$$

$$\text{EMP}_2 = \text{EMP} \bowtie \text{PAY}_2$$

where

$$\text{PAY}_1 = \sigma_{\text{SAL} \leq 30000}(\text{PAY})$$

$$\text{PAY}_2 = \sigma_{\text{SAL} > 30000}(\text{PAY})$$

PAY₁

TITLE	SAL
Mech. Eng.	27000
Programmer	24000

PAY₂

TITLE	SAL
Elect. Eng.	40000
Syst. Anal.	34000

EMP₁

ENO	ENAME	TITLE
E3	A. Lee	Mech. Eng.
E4	J. Miller	Programmer
E7	R. Davis	Mech. Eng.

EMP₂

ENO	ENAME	TITLE
E1	J. Doe	Elect. Eng.
E2	M. Smith	Syst. Anal.
E5	B. Casey	Syst. Anal.
E6	L. Chu	Elect. Eng.
E8	J. Jones	Syst. Anal.

VF – Information Requirements

■ Application Information

▢ Attribute affinities

- ◆ a measure that indicates how closely related the attributes are
- ◆ This is obtained from more primitive usage data

▢ Attribute usage values

- ◆ Given a set of queries $Q = \{q_1, q_2, \dots, q_q\}$ that will run on the relation $R[A_1, A_2, \dots, A_n]$,

$$use(q_i, A_j) = \begin{cases} 1 & \text{if attribute } A_j \text{ is referenced by query } q_i \\ 0 & \text{otherwise} \end{cases}$$

$use(q_i, \bullet)$ can be defined accordingly

VF – Information Requirements

Consider the following 4 queries for relation PROJ

q_1 : **SELECT** BUDGET
FROM PROJ
WHERE PNO=Value

q_2 : **SELECT** PNAME,BUDGET
FROM PROJ

q_3 : **SELECT** PNAME
FROM PROJ
WHERE LOC=Value

q_4 : **SELECT** SUM(BUDGET)
FROM PROJ
WHERE LOC=Value

Let A_1 = PNO, A_2 = PNAME, A_3 = BUDGET, A_4 = LOC

	A_1	A_2	A_3	A_4
q_1	1	0	1	0
q_2	0	1	1	0
q_3	0	1	0	1
q_4	0	0	1	1

Algorithm: 1. Affinity Measure $aff(A_i, A_j)$

The **attribute affinity measure** between two attributes A_i and A_j of the relation $R[A_1, A_2, \dots, A_n]$ with respect to the set of applications/queries $Q = \{q_1, q_2, \dots, q_q\}$ is defined as follows:

$$aff(A_i, A_j) = \sum_{k | use(q_k, A_i) = 1 \wedge use(q_k, A_j) = 1} \sum_{\forall R_l} ref_l(q_k) \times acc_l(q_k)$$

where R_l is a fragment of R in site S_l , $ref_l(q_k)$ is the number of access to attributes (A_i, A_j) for each execution of the query q_k at site S_l and $acc_l(q_k)$ is the query access frequency measure

Algorithm: 2. Affinity Matrix AA

Assume each query in the previous example accesses the attributes once during each execution.

Also assume the access frequencies



	S_1	S_2	S_3
q_1	15	20	10
q_2	5	0	0
q_3	25	25	25
q_4	3	0	0

Then

$$\begin{aligned} aff(A_1, A_3) &= 15*1 + 20*1 + 10*1 \\ &= 45 \end{aligned}$$

and the attribute affinity matrix AA is



	A_1	A_2	A_3	A_4
A_1	45	0	45	0
A_2	0	80	5	75
A_3	45	5	53	3
A_4	0	75	3	78

Algorithm: 3. BEA to Reorder AA

- Take the attribute affinity matrix AA and reorganize the attribute orders to form clusters where the attributes in each cluster demonstrate high affinity to one another.
- **Bond Energy Algorithm** (BEA) has been used for clustering of entities. BEA finds an ordering of entities (in our case attributes) such that the global affinity measure

$$AM = \sum_i \sum_j (\text{affinity of } A_i \text{ and } A_j \text{ with their neighbors})$$

is maximized.

Affinity Measure

$$AM = \sum_{i=1}^n \sum_{j=1}^n aff(A_i, A_j) [aff(A_i, A_{j-1}) + aff(A_i, A_{j+1}) + aff(A_{i-1}, A_j) + aff(A_{i+1}, A_j)]$$

Boundary conditions:

$$aff(A_0, A_j) = aff(A_i, A_0) = aff(A_{n+1}, A_j) = aff(A_i, A_{n+1}) = 0$$

And since the AA matrix is symmetric, we revise the definition of affinity measure to:

$$AM = \sum_{i=1}^n \sum_{j=1}^n aff(A_i, A_j) [aff(A_i, A_{j-1}) + aff(A_i, A_{j+1})]$$

Bond Energy Algorithm (BEA)

Input: The AA matrix

Output: The clustered affinity matrix CA which is a perturbation of AA

- ① *Initialization*: Place and fix one of the columns of AA in CA .
- ② *Iteration*: Place the remaining $n-i$ columns in the remaining $n-i$ positions in the CA matrix. For each column, choose the placement that makes the most contribution to the global affinity measure.
- ③ *Row order*: Order the rows according to the column ordering.

Bond Energy Algorithm (BEA)

$$\begin{array}{c}
 AA = \\
 \begin{array}{c}
 A_1 \\
 A_2 \\
 A_3 \\
 A_4
 \end{array}
 \begin{array}{c}
 A_1 \ A_2 \ A_3 \ A_4 \\
 \left[\begin{array}{cccc}
 45 & 0 & 45 & 0 \\
 0 & 80 & 5 & 75 \\
 45 & 5 & 53 & 3 \\
 0 & 75 & 3 & 78
 \end{array} \right]
 \end{array}
 \end{array}
 \longrightarrow
 \begin{array}{c}
 CA = \\
 \begin{array}{c}
 A_1 \\
 A_3 \\
 A_2 \\
 A_4
 \end{array}
 \begin{array}{c}
 A_1 \ A_3 \ A_2 \ A_4 \\
 \left[\begin{array}{cccc}
 45 & 45 & 0 & 0 \\
 45 & 53 & 5 & 3 \\
 0 & 5 & 80 & 75 \\
 0 & 3 & 75 & 78
 \end{array} \right]
 \end{array}
 \end{array}$$

At each step i :

$$\underbrace{A_1 \ A_2 \ \dots \ A_r \ A_{r+1} \ \dots \ A_i}_{AM_{old}} \longrightarrow \underbrace{A_1 \ A_2 \ \dots \ A_r \ A_t \ A_{r+1} \ \dots \ A_i}_{AM_{new}}$$

$$cont(A_r, A_t, A_{r+1}) = AM_{new} - AM_{old}$$

Bond Energy Algorithm (BEA)

Define $bond(A_x, A_y)$:

$$bond(A_x, A_y) \equiv \sum_{z=1}^n aff(A_z, A_x) \times aff(A_z, A_y)$$

But:

$$\begin{aligned} AM &= \sum_{i=1}^n \sum_{j=1}^n aff(A_i, A_j) [aff(A_i, A_{j-1}) + aff(A_i, A_{j+1})] \\ \Rightarrow AM &= \sum_{j=1}^n [bond(A_j, A_{j-1}) + bond(A_j, A_{j+1})] \end{aligned}$$

Do the math:

$$\begin{aligned} cont(A_r, A_t, A_{r+1}) &= AM_{new} - AM_{old} \\ &= 2bond(A_r, A_t) + 2bond(A_t, A_{r+1}) - 2bond(A_r, A_{r+1}) \end{aligned}$$

BEA Example

Consider the following AA matrix and the corresponding CA matrix where A_1 and A_2 have been placed. Place A_3 :

$$AA = \begin{matrix} & \begin{matrix} A_1 & A_2 & A_3 & A_4 \end{matrix} \\ \begin{matrix} A_1 \\ A_2 \\ A_3 \\ A_4 \end{matrix} & \begin{bmatrix} 45 & 0 & 45 & 0 \\ 0 & 80 & 5 & 75 \\ 45 & 5 & 53 & 3 \\ 0 & 75 & 3 & 78 \end{bmatrix} \end{matrix} \quad CA = \begin{matrix} & \begin{matrix} A_1 & A_2 \end{matrix} \\ \begin{matrix} A_1 \\ A_2 \\ A_3 \\ A_4 \end{matrix} & \begin{bmatrix} 45 & 0 \\ 0 & 80 \\ 45 & 5 \\ 0 & 75 \end{bmatrix} \end{matrix}$$

Ordering (0-3-1) :

$$\begin{aligned} cont(A_0, A_3, A_1) &= 2bond(A_0, A_3) + 2bond(A_3, A_1) - 2bond(A_0, A_1) \\ &= 2 * 0 + 2 * 4410 - 2 * 0 = 8820 \end{aligned}$$

Ordering (1-3-2) :

$$\begin{aligned} cont(A_1, A_3, A_2) &= 2bond(A_1, A_3) + 2bond(A_3, A_2) - 2bond(A_1, A_2) \\ &= 2 * 4410 + 2 * 890 - 2 * 225 = 10150 \end{aligned}$$

Ordering (2-3-4) :

$$cont(A_2, A_3, A_4) = 1780$$

BEA Example

Therefore, the CA matrix has to form

$$\begin{array}{ccc} A_1 & A_3 & A_2 \\ \left[\begin{array}{ccc} 45 & 45 & 0 \\ 0 & 5 & 80 \\ 45 & 53 & 5 \\ 0 & 3 & 75 \end{array} \right] \end{array}$$

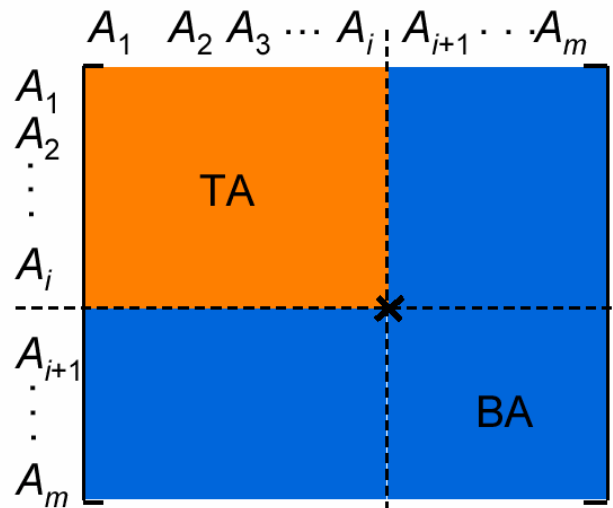
BEA Example

When A_4 is placed, the final form of the CA matrix (after row organization) is

	A_1	A_3	A_2	A_4
A_1	45	45	0	0
A_3	45	53	5	3
A_2	0	5	80	75
A_4	0	3	75	78

Algorithm: 4. Clustering CA

How can you divide a set of clustered attributes $\{A_1, A_2, \dots, A_n\}$ into two (or more) sets $\{A_1, A_2, \dots, A_i\}$ and $\{A_i, \dots, A_n\}$ such that there are no (or minimal) applications that access both (or more than one) of the sets.



Clustering Measure

Define

TQ = set of applications that access only TA

BQ = set of applications that access only BA

OQ = set of applications that access both TA and BA

and

$$C_{xx} = \sum_{q_i \in xx} \sum_{\forall S_l} ref_l(q_i) \times acc_l(q_i)$$

CTQ = total number of accesses to attributes by applications that access only TA

CBQ = total number of accesses to attributes by applications that access only BA

COQ = total number of accesses to attributes by applications that access both TA and BA

Then find the point along the diagonal that maximizes

$$CTQ * CBQ - COQ^2$$

Clustering Problems

Two problems :

❶ Cluster forming in the middle of the CA matrix

- ➡ Shift a row up and a column left and apply the algorithm to find the “best” partitioning point
- ➡ Do this for all possible shifts
- ➡ Cost $O(m^2)$

❷ More than two clusters

- ➡ m -way partitioning
- ➡ try 1, 2, ..., $m-1$ split points along diagonal and try to find the best point for each of these
- ➡ Cost $O(2^m)$

VF – Correctness

A relation R , defined over attribute set A and key K , generates the vertical partitioning $F_R = \{R_1, R_2, \dots, R_r\}$.

■ Completeness

➡ The following should be true for A :

$$A = \bigcup A_{R_i}$$

■ Reconstruction

➡ Reconstruction can be achieved by

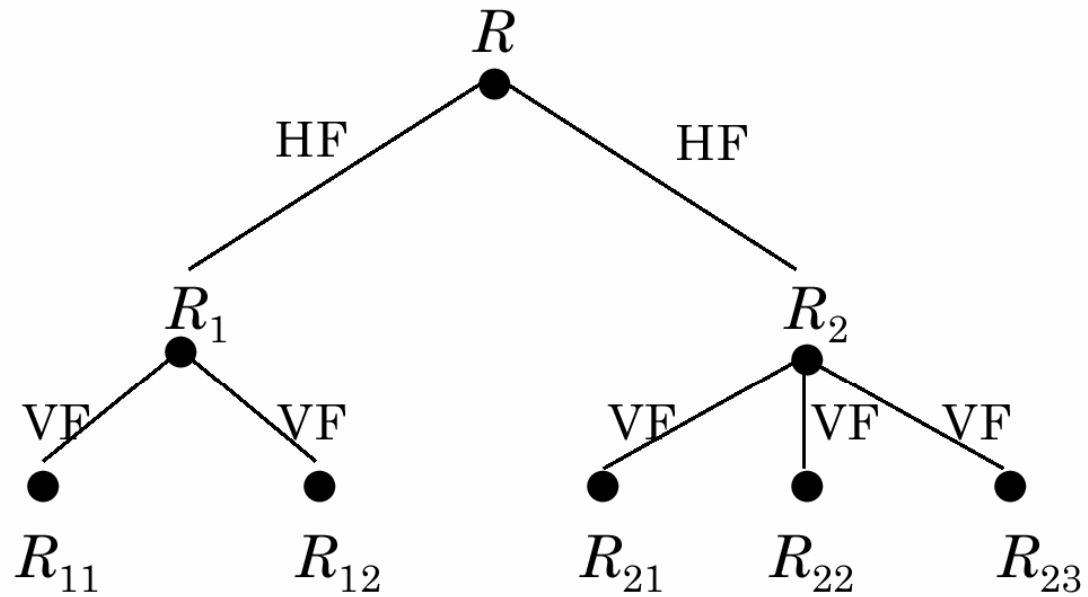
$$R = \bowtie_K R_i \quad \forall R_i \in F_R$$

■ Disjointness

➡ TID's are not considered to be overlapping since they are maintained by the system

➡ Duplicated keys are not considered to be overlapping

Hybrid Fragmentation



Outline

- Design what?
- Fragmentation
- Allocation

Fragment Allocation Problem

■ Problem Statement

Given

$F = \{F_1, F_2, \dots, F_n\}$	fragments
$S = \{S_1, S_2, \dots, S_m\}$	network sites
$Q = \{q_1, q_2, \dots, q_q\}$	applications

Find the "optimal" distribution of F to S .

■ Optimality

➤ Minimal cost

- ◆ Communication + storage + processing (read & update)
- ◆ Cost in terms of time (usually)

➤ Performance

Response time and/or throughput

➤ Constraints

- ◆ Per site constraints (storage & processing)

Information Requirements

- Database information
 - selectivity of fragments
 - size of a fragment
- Application information
 - access types and numbers
 - access localities
- Communication network information
 - unit cost of storing data at a site
 - unit cost of processing at a site
- Computer system information
 - bandwidth
 - latency
 - communication overhead

Allocation Solution

- DAP is NP-complete

- Heuristics based on

- single commodity warehouse location
- knapsack problem
- branch and bound techniques
- network flow